

October 30

SWBAT:

Find the area between
two curves

Find the area
bounded by
 $f(x) = 3\cos x$
 $g(x) = \sin x - 4$
on the interval
 $(1, 2\pi)$

Find the area bounded by $f(x) = 3\cos x$, $g(x) = \sin x - 4$
on the interval $[1, 2\pi]$

$$A = \int_1^{2\pi} (3\cos x - (\sin x - 4)) dx = 19.068$$

Find the area bounded by
 $f(x) = 3\cos(x)$
 $g(x) = \sin(x) - 4$
on interval $(1, 2\pi)$

$$A = \int_1^{2\pi} (3\cos(x) - (\sin(x) - 4)) dx$$

$$19.068$$

$$f(x) = 3\cos x$$

$$g(x) = \sin x - 4$$

$$\int_1^{2\pi} 3\cos x dx$$

$$3\sin x \Big|_1^{2\pi}$$

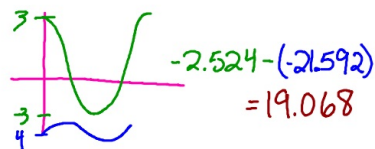
$$3\sin(2\pi) - 3\sin(1)$$

$$= -2.524$$

$$\int_1^{2\pi} (\sin x - 4) dx = -\cos(2\pi) - 4(2\pi) - (-\cos(1) - 4(1))$$

$$= -\cos(2\pi) - 4(2\pi) + \cos(1) + 4(1)$$

$$= -27.068$$



Area between curves

$$A = \int_a^b \underset{\substack{\text{upper} \\ y \\ \text{top}}}{\quad} - \underset{\substack{\text{lower} \\ y \\ \text{bottom}}}{\quad} dx$$

Find the area enclosed by

$$y = 4\sin\left(\frac{\pi x}{3}\right)$$

and

$$y = -(x-3)^2 + 5$$

on the interval

[2, 5]

.
.

$$\text{fnInt}(\text{function}, X, \text{lower}, \text{upper})$$

$$\int_2^5 \left(-(x-3)^2 + 5 \right) - \left(4\sin\left(\frac{\pi x}{3}\right) \right) dx$$

$$= 15.820$$

$$15.819$$

Find the area enclosed by

$$y = 4\sin\left(\frac{\pi x}{3}\right)$$

and

$$y = -(x - 3)^2$$

bounds are at
intersection points

$$(3, 0) \text{ and } (4.90799, -3.6404)$$

$$\int_3^{4.90799} -(x-3)^2 - 4\sin\left(\frac{\pi x}{3}\right) dx$$
$$= 3.087$$

Find the area enclosed by

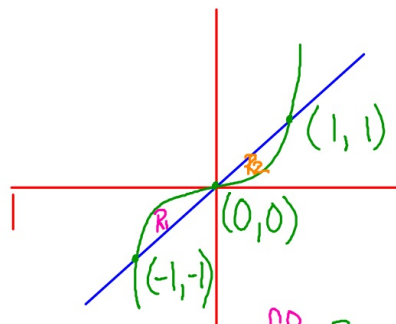
$$f(x) = 0.5x^3 \text{ and}$$

$$g(x) = 5 - x^4$$

$$12.1773$$

$$A = \int_{-1.6379}^{1.3844} g(x) - f(x) dx$$

Find the area
enclosed by
 $f(x) = x^3$ and
 $g(x) = x$



$$\int_{-1}^0 x^3 - x \, dx + \int_0^1 x - x^3 \, dx = \frac{1}{2}$$