

September 4
 SWBAT:
 Use summation notation
 to find the Riemann Sum

- 1) Write an equation of the line with slope = 2 and goes through the point (1, 5).

$$y - y_1 = m(x - x_1)$$

$$y - 5 = 2(x - 1)$$

$$y = 2x + 3$$

$$y = 5 + 2(x - 1)$$

- 2) Solve: $2x^2 - 18 = 0$

$$2x^2 - 18 = 0$$

$$+18 +18$$

$$2x^2 = 18$$

$$\frac{2x^2}{2} = \frac{18}{2}$$

$$x^2 = 9$$

$$\sqrt{x^2} = \sqrt{9}$$

$$x = 3 \text{ AND } x = -3$$

- 3) Solve: $x^3 + 2 = 10$

$$x^3 + 2 = 10$$

$$\frac{-2 \quad -2}{-2 \quad -2}$$

$$x^3 = 8$$

$$\sqrt[3]{x^3} = \sqrt[3]{8}$$

$$x = 2$$

$$x = \sqrt[3]{8}$$

- 4) Factor: $2x^2 - 24x$

$$2x^2 - 24x = 2x(x - 12)$$

$$2(x^2 - 12x)$$

$$x(2x - 24)$$

$$(2x + 0)(x - 12)$$

- 5) Solve: $\frac{3x-7}{x} = 2$

$$\frac{3x-7}{x} = 2 \cdot x$$

$$3x-7 = 2x$$

$$-7 = -x$$

$$7 = x$$

$$\frac{3x-7}{x} = \frac{2}{1}$$

$$3 - \frac{7}{x} = 2$$

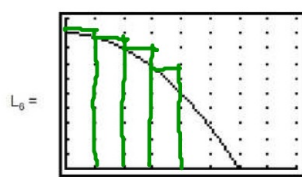
$$\frac{3x}{x} - \frac{7}{x}$$

Can you cancel the 3x and x?

$$-\frac{7}{x} = -1$$

1. Let $f(x) = 9 - x^2$ on $[0,3]$

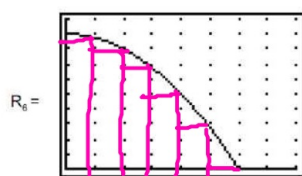
- a) If all intervals are the same width are there six rectangles, what is the value of Δx ? _____.
Use this value to compute the following.



Left-hand Rule

20.125

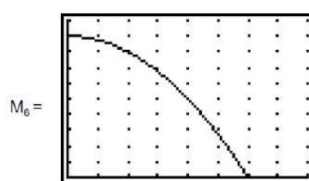
Interval	x-value	y-value/ height	Width	area



Right-hand Rule

15.625

Interval	x-value	y-value/ height	Width	area



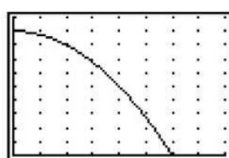
Midpoint Rule

17.525

Interval	x-value	y-value/ height	Width	area

Homework - Due Friday

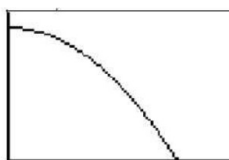
- b) Suppose Δx has width equal 0.5. Chose a random value for x_k in each interval and compute the area of each Riemann rectangle. Find the total of the rectangles.



Random x-coordinate

Interval	x-value	y-value/ height	Width	area

- c) Choose six randomly sized intervals and choose a point at random in each interval. Compute the area of the Riemann rectangle and find the total area.



Random rectangles

Interval	x-value	y-value/ height	Width	area

2. Let $f(x) = 3^x$ on $[-1,3]$

- a) Find
 $L_8 =$
 $R_8 =$
 $M_8 =$

width?

8 rectangles
width = $.5 = \frac{3 - (-1)}{8} = \frac{4}{8}$

- ~~b) Suppose Δx has width equal 0.5. Chose a random value for x_k in each interval and compute the area of each Riemann rectangle. Find the total area approximated by the rectangles.~~
~~c) Choose eight randomly sized intervals and choose a point at random in each interval. Compute the area of the Riemann rectangle and find the total area approximated by the rectangles.~~

Summation
Notation

$$\sum_{x=a}^b f(x)$$

sum of $f(x)$ from $x=a$ to b
└──────────┘
 positive
whole #s

$$\sum_{x=1}^4 x = 1 + 2 + 3 + 4 = 10$$

$$\sum_{x=2}^5 x^2 = 2^2 + 3^2 + 4^2 + 5^2$$

$$= 4 + 9 + 16 + 25 = 54$$

$$\sum_{x=1}^3 2x - 5$$

$$(2(1)-5) + (2(2)-5) + (2(3)-5)$$

$$-3 + -1 + 1 = -3$$

write in
summation
notation

$$2^1 + 2^2 + 2^3 + 2^4$$

$$+ 2^5 + 2^6$$

$$= \sum_{x=1}^6 2^x$$

$$\sin(3\pi) + \sin(4\pi)$$

$$+ \sin(5\pi) + \sin(6\pi)$$

$$= \sum_{x=3}^6 \sin(x\pi)$$

Let $f(x) = 9 - x^2$ on $[0, 3]$

- a) If all intervals are the same width and there are six rectangles, what is the value of Δx_k ? _____.
Use this value to compute the following.



Interval	x-value	y-value/ height	Width	area
	0	$9 - 0^2$.5	
	.5	$9 - .5^2$.5	
	1	$9 - 1^2$.5	
	1.5	$9 - 1.5^2$.5	
	2	$9 - 2^2$.5	
	2.5	$9 - 2.5^2$.5	

$$\begin{aligned}
 &.5(9 - 0^2) + .5(9 - .5^2) + .5(9 - 1^2) + .5(9 - 1.5^2) \\
 &\quad + .5(9 - 2^2) + .5(9 - 2.5^2) \\
 &= .5(9 - 0^2) + .5(9 - (\frac{1}{2})^2) + .5(9 - (\frac{2}{2})^2) \\
 &\quad + .5(9 - (\frac{3}{2})^2) + .5(9 - (\frac{4}{2})^2) + .5(9 - (\frac{5}{2})^2) \\
 &= \sum_{x=0}^5 .5(9 - (\frac{x}{2})^2)
 \end{aligned}$$