

Joe is filling up his pool. Water flows out of the hose into a pool at a rate ^{→ derivative} modeled by the equation:

$$f(x) = 0.7x^3 - 3x + 7, \text{ where } x \text{ is measured in hours.}$$

If there are 10 gallons of water in the pool when he starts filling it up, how much is in the pool after 5 hours? ~~= 116.875~~

$$f(x) = 0.7x^3 - 3x + 7 = I'(x) \quad (0, 10) \quad (\text{time, Amount})$$

→ Amount = \int rate ← bounds = 0 to 5

$$\begin{aligned} A &= \int_0^5 .7x^3 - 3x + 7 \, dx = \left. \frac{.7x^4}{4} - \frac{3x^2}{2} + 7x \right|_0^5 = \frac{.7(5)^4}{4} - \frac{3(5)^2}{2} + 7(5) - \left(\frac{.7(0)^4}{4} - \frac{3(0)^2}{2} + 7(0) \right) \\ &= .7 \int_0^5 x^3 \, dx - 3 \int_0^5 x \, dx + \int_0^5 7 \, dx \\ &= .7 \left(\frac{x^4}{4} \Big|_0^5 \right) - 3 \left(\frac{x^2}{2} \Big|_0^5 \right) + 7x \Big|_0^5 = .7 \left(\frac{5^4}{4} - \frac{0^4}{4} \right) - 3 \left(\frac{5^2}{2} - \frac{0^2}{2} \right) + (7(5) - 7(0)) \\ &= 106.875 \text{ gallons} + 10 \end{aligned}$$