

September 7

SWBAT:

Determine when the area under a curve will be positive, negative, or zero and apply properties of definite integrals.



6. Based on your observations on pages 1.2 and 2.2, for any continuous function f on an interval $[c, d]$ and for a and b in $[c, d]$, when will the definite integral $\int_a^b f(x) dx$ be positive? Negative? Zero? Clearly explain your generalization.

Positive

$b > a$ + there is more area above the x-axis

$b < a$ + there is more area under the x-axis

Negative

$b < a$ + there is more area above the x-axis

$b > a$ + there is more area below the x-axis

Zero: $b = a$

or the area above
= the area below

Order of Integration	$\int_a^b f(x) \, dx = -\int_b^a f(x) \, dx$
Zero	$\int_a^a f(x) \, dx = 0$
Constant Multiple	$\int_a^b k \cdot f(x) \, dx = k \int_a^b f(x) \, dx$ For any number k
Additivity	$\int_a^b f(x) \, dx + \int_b^c f(x) \, dx = \int_a^c f(x) \, dx$
Constant Multiple (special case)	$\int_a^b -f(x) \, dx = -\int_a^b f(x) \, dx \quad k = -1$
Sum and Difference	$\int_a^b f(x) \pm g(x) \, dx = \int_a^b f(x) \, dx \pm \int_a^b g(x) \, dx$

Quotient Rule

Product Rule