

February 10

(Move one seat to the left and one seat up - if you were in the first row, move to the third row.)

What is a limit and how do you find it?



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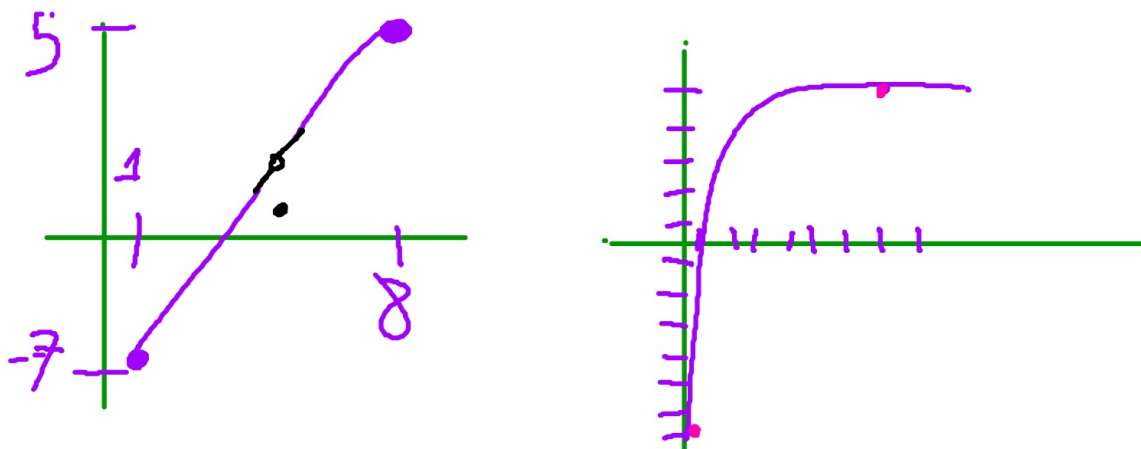
Students will verbally explain how to apply the Intermediate Value Theorem to Justify solutions

(using the words:  
value, continuous, exist...)



Let the two points  $(1, -7)$  and  $(8, 5)$  be two points on the graph of a given function  $F$ .  
 Let the domain of  $F$  include all numbers  $1 \leq x \leq 8$ .

Sketch what the graph of  $f$  might look like that meets the two conditions listed above.

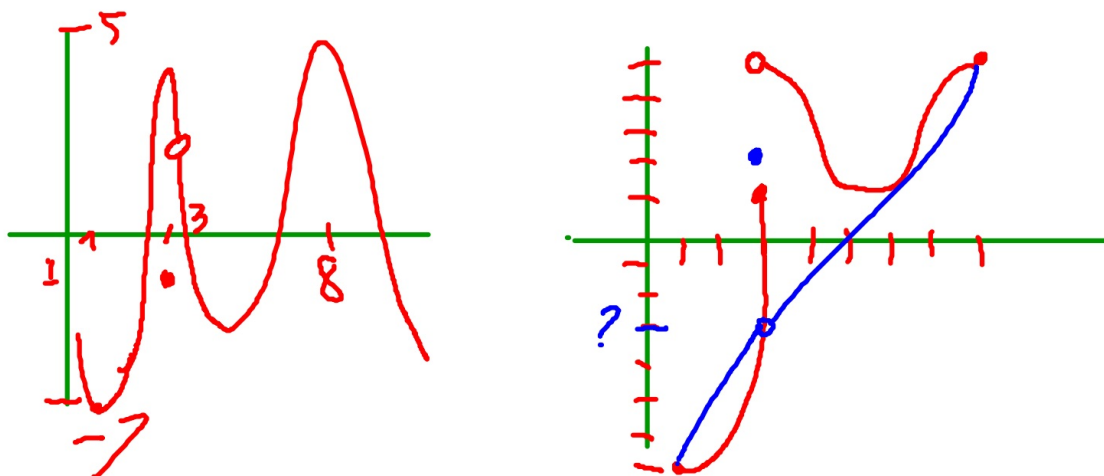


Let the two points  $(1, -7)$  and  $(8, 5)$  be two points on the graph of a given function  $G$ .  
 Let the domain of  $G$  include all numbers  $1 \leq x \leq 8$

Let  $G$  not be continuous at  $x = 3$ .

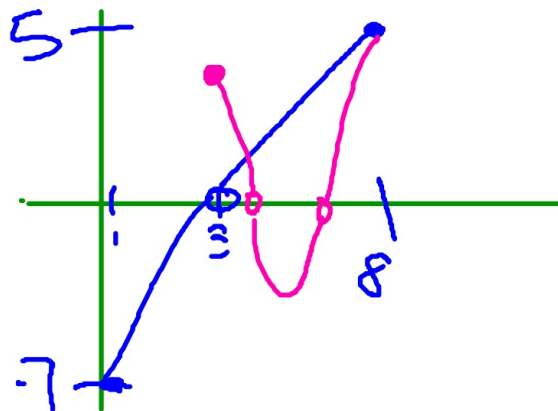
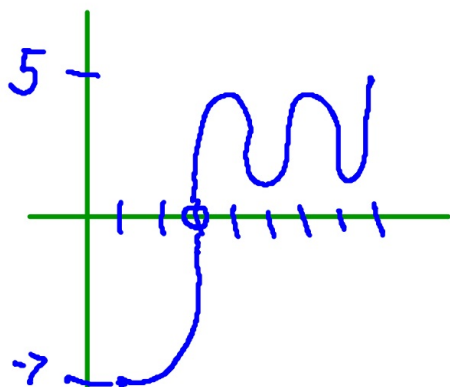
Let the range of  $G$  be every number such that  $-7 \leq y \leq 5$ .

Sketch what the graph of  $G$  might look like.



Let the two points  $(1, -7)$  and  $(8, 5)$  be two points on the graph of a given function  $H$ .  
 Let the domain of  $H$  include all numbers  $1 \leq x \leq 8$   
 Let  $H$  not be continuous at  $x = 3$ .  
 Let the range of  $H$  be every number such that  $-7 \leq y < 0$  and  $0 < y \leq 5$ .

Sketch what the graph of  $H$  might look like.



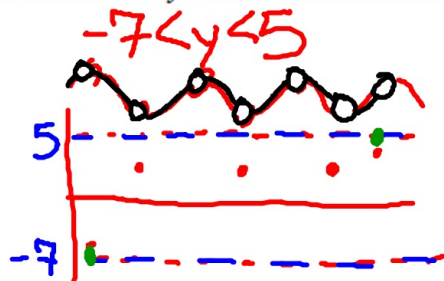
Statement 1: If  $(1, -7)$  and  $(8, 5)$  are on the graph of some function  $J$  and if  $J$  is continuous at every number in the open interval  $1 < x < 8$  then 4 must be in the range of  $J$ .

True

Statement 2: If  $(1, -7)$  and  $(8, 5)$  are on the graph of some function  $K$  and for every number  $x$  in the  $1 \leq x \leq 8$  there may be some number  $y$  in the interval  $-7 < y < 5$  which is not in the range of  $K$ .

True

$K$  does not have to be continuous



Statement 3: If the two points  $(a, b)$  and  $(c, d)$  are on the graph of some function  $I$ , what conditions must be met by the function  $I$  to guarantee that there exists a point  $(e, f)$  such that  $a < e < b$  and  $b < f < d$ .

$a < e < c$  and  $b < f < d$

$(1, -7)$   $1 < e < 8$   
 $(8, 5)$   $-7 < f < 5$

## The Intermediate Value Theorem (IVT)

If a function  $f$  is continuous on a closed interval  $[a, b]$ , and  $f(a) \neq f(b)$ , then for every value of  $u$  between  $f(a)$  and  $f(b)$ , there exist at least one value of  $c$  in the open interval  $(a, b)$  so that  $f(c) = u$ .

