

February 25

If $f'(1) = -7$ and $f(1) = 10$, write an equation of a line tangent to $f(x)$ at $x = 1$.

$$x = 1$$

$$y = 10$$

$$\text{slope} = -7$$

$$y - 10 = -7(x - 1)$$

$$y = -7x + 17$$



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Students will verbally explain how to find derivative, using the definition of the derivative.

(using the words:
limit, expand, simplify...)



Definition of the Derivative

$$\lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} = f'(x)$$

$$y = x^2 - 7x + 20$$

Find $\frac{dy}{dx}$

$(y', f'(x))$

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$f(x) = x^2 - 7x + 20$$

$$f(x+h) = (x+h)^2 - 7(x+h) + 20$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{(x+h)^2 - 7(x+h) + 20 - (x^2 - 7x + 20)}{h}$$

$$\lim_{h \rightarrow 0} \frac{(x+h)(x+h) - 7x - 7h + 20 - x^2 + 7x - 20}{h}$$

$$\lim_{h \rightarrow 0} \frac{x^2 + 2xh + h^2 - 7x - 7h + 20 - x^2 + 7x - 20}{h}$$

$$\lim_{h \rightarrow 0} \frac{2xh + h^2 - 7h}{h} = \lim_{h \rightarrow 0} \frac{h(2x + h - 7)}{h}$$

$$\lim_{h \rightarrow 0} 2x + h - 7 = 2x - 7$$

$$f'(x) = 2x - 7$$

Pg 125 #3, 5 (only use EQ 1), 19, 20, 27, 29, 31, 33, 35, 51 – 56 (all)

In Exercises 3–6, compute $f'(a)$ in two ways, using Eq. (1) and Eq. (2).

3. $f(x) = x^2 + 9x, a = 0$

Show Answer

In Exercises 27–44, use the limit definition to compute $f'(a)$ and find an equation of the tangent line.

4. $f(x) = x^2 + 9x, a = 2$

27. $f(x) = 2x^2 + 10x, a = 3$

5. $f(x) = 3x^2 + 4x + 2, a = -1$

Show Answer

28. $f(x) = 4 - x^2, a = -1$

29. $f(t) = t - 2t^2, a = 3$

Show Answer