

A photograph of a green and yellow train stopped at a station platform. The train is facing the viewer, and the platform is visible on the left. The background shows a building and a cloudy sky.

March 19

How is the speed of a car related
to the position of a car?

A photograph of a green and yellow train stopped at a station platform. The train is facing the viewer, and the platform is visible on the left. The background shows a building and a cloudy sky.

March 19

Students will verbally explain how to
find and interpret velocity and
acceleration functions
(using the words:
rate of change, derivative...)

| | |
|------------------------|--|
| Position Function | $s(t)$ |
| Displacement | Change in Position final position - starting position |
| Average Velocity | Average Rate of Change $\frac{\text{Change in Position}}{\text{Change in time}} = \frac{s(b) - s(a)}{b - a}$ |
| Instantaneous Velocity | <ul style="list-style-type: none"> - Instantaneous Rate of Change in position - Derivative of Position = $s'(t) = v(t)$ - If positive, then it is moving right/up/forward - If negative, then it is moving left/down/backward |
| Speed | Absolute Value of Velocity = $ s'(t) = v(t) $ |
| Acceleration | Instantaneous Change in Velocity <ul style="list-style-type: none"> - Derivative of Velocity = $v'(t) = a(t)$ - 2nd Derivative of Position = $s''(t) = a(t)$ |

The position of an object is given by
 $s(t) = t^3 - 12t^2 + 45t - 6$

Find the average velocity on $[0, 3]$
 $0 \leq t \leq 3$

change in position → slope of secant line
 change in time

$$\begin{aligned} \frac{s(0) - s(3)}{0 - 3} &= \frac{(0^3 - 12(0)^2 + 45(0) - 6) - (3^3 - 12(3)^2 + 45(3) - 6)}{0 - 3} \\ &= \frac{-6 - 48}{-3} = \frac{-54}{-3} = 18 \end{aligned}$$

average velocity

find the instantaneous velocity at $t = 4$

derivative of position

$$s'(t) = v(t) = 3t^2 - 24t + 45$$

$$v(4) = 3(4)^2 - 24(4) + 45 = -3$$

instantaneous velocity

find the function that models the acceleration.

second derivative of position

first derivative of velocity

$$s''(t) = v'(t) = a(t) = 6t - 24$$